

# Cogenhoe Primary School

## Calculation Policy

This calculation policy has been written to ensure consistency and progression across the school in the teaching and learning of the four operations in Mathematics.

### The Aim -

- 1) For children to be shown a range of calculation methods throughout their time at Cogenhoe.
- 2) For children to engage in a two-way dialogue with teachers and peers about the methods being used.
- 3) For children to select preferred methods and to have the confidence to use these methods independently.


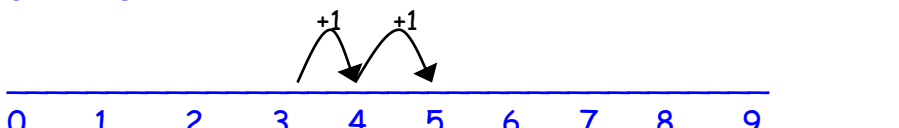
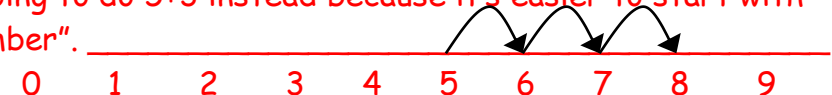

### Points to remember

**Use of Number lines** - jumps should be shown on the number line - with jumps above the number line for addition and under the number line for subtraction.


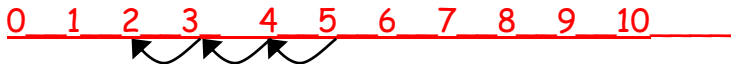
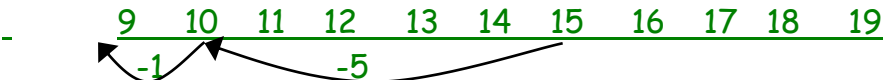
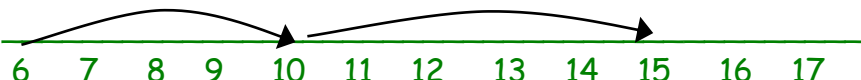
**The inverse** - children should be encouraged (when appropriate) to use the inverse for checking subtraction and division.

## Calculation Policy- Addition

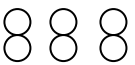
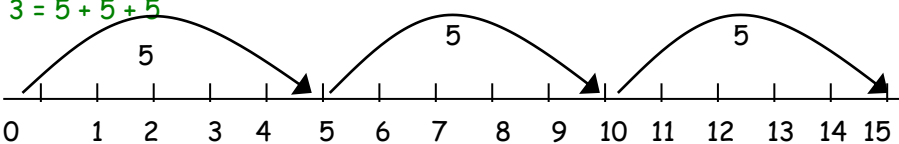
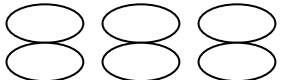
### By the end of each Stage:

<p><b>EYFS Stage</b> -To be able to use quantities and objects to add two single digit numbers and count on to find the answer.</p> <div style="text-align: center;">  <p><math>3 + 2 = 5</math></p>  </div>	<p><b>Stage 1</b> -To be able to add one digit and two digit numbers to 20 including 0.</p> <p><b>Always start with the biggest number and count on</b>  <math>3 + 5 =</math> "I'm going to do <math>5+3</math> instead because it's easier to start with the bigger number".</p> 			
<p><b>Stage 2</b> -To begin to move from a pictorial representations to a more formal columnar method.</p> <p><b>Bridging 10s</b>-break down the units <math>19 + 13 = 19 + 1 + 2 + 10 = 32</math></p>  <p><b>NB</b> - 100 squares and Base 10 materials to be used too.</p> <p><b>Partitioned column method.</b> <math>67 + 42 =</math></p> $\begin{array}{r} 60 + 7 \\ 40 + 2 \\ \hline 100 + 9 = 109 \end{array}$	<p><b>Stage 3</b> -To be able to add numbers with up to 3 digits using a formal written method of columnar addition.</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; padding: 5px;"> <p><b>Partitioned informal method</b></p> <math>267 + 127 = ?</math>  <math>O \ 7 + 7 = 14</math>  <math>T \ 60 + 20 = 80</math>  <math>H \ 200 + 100 = 300</math>  <math>14 + 80 + 300 =</math>  <math>380 + 10 + 4 = 394</math> </td> <td style="width: 50%; padding: 5px;"> <p><b>Partitioned column method.</b></p> <math display="block">\begin{array}{r} 200 + 60 + 7 \\ 100 + 20 + 7 \\ \hline 300 + 80 + 14 \\ \hline 394 \end{array}</math> </td> </tr> </table>	<p><b>Partitioned informal method</b></p> $267 + 127 = ?$ $O \ 7 + 7 = 14$ $T \ 60 + 20 = 80$ $H \ 200 + 100 = 300$ $14 + 80 + 300 =$ $380 + 10 + 4 = 394$	<p><b>Partitioned column method.</b></p> $\begin{array}{r} 200 + 60 + 7 \\ 100 + 20 + 7 \\ \hline 300 + 80 + 14 \\ \hline 394 \end{array}$	
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<p><b>Stage 4</b>-To be able to add numbers with up to 4 digits using an extended column method.</p>	<p><b>Stage 5</b> - To be able to add whole numbers and decimals with more than 4 digits using a compact written method (column addition).</p>	<p><b>Stage 6</b>-To be able to solve addition and subtraction multi step problems in context, deciding which methods to use and why.</p>		
$\begin{array}{r} 1267 \\ + 2127 \\ \hline 14 \text{ (7+7)} \\ 80 \text{ (60 + 20)} \\ 300 \text{ (200+100)} \\ \hline 3000 \text{ (1000+2000)} \\ \hline 3394 \end{array}$	<table style="width: 100%;"> <tr> <td style="width: 50%; text-align: center;"> <math display="block">\begin{array}{r} 1358 \\ + 3473 \\ \hline 4831 \\ 11 \end{array}</math> </td> <td style="width: 50%; text-align: center;"> <math display="block">\begin{array}{r} 1.358 \\ + 3.473 \\ \hline 4.831 \\ 11 \end{array}</math> </td> </tr> </table>	$\begin{array}{r} 1358 \\ + 3473 \\ \hline 4831 \\ 11 \end{array}$	$\begin{array}{r} 1.358 \\ + 3.473 \\ \hline 4.831 \\ 11 \end{array}$	
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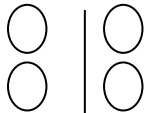
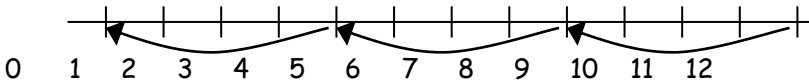
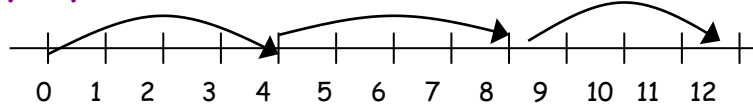
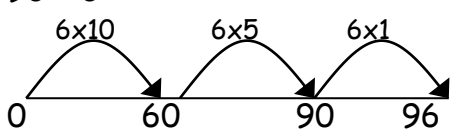
## Calculation Policy - Subtraction

<p><b>EYFS Stage</b> - To be able to use quantities and objects to subtract two single digit numbers and count back to find the answer.</p>	<p><b>Stage 1-</b> To be able to subtract one digit and two digit numbers to 20 including 0.</p>																																													
<p><b>Counting Back</b> Understand subtraction as 'taking away'</p>  <p>three take away 2 leaves....1 dog.</p>	<p>You can count backwards on a number line. <math>5-3 = 2</math></p>  <p>-1 -1 -1 OR start with 3 and count on to 5. The difference is 2.</p>																																													
<p><b>Stage 2</b> - To be able to subtract numbers with up to 2 digits using a number line.</p>	<p><b>Stage 3</b> - To be able to subtract 3-digit numbers using a partitioned written method.</p>																																													
<p><b>2. Using a number line to take away - bridging tens.</b>  <math>15 - 6 = 15 - 5 - 1 = 9</math></p>  <p><b>Count up - subtraction as finding the difference</b></p> 	<p><b>Horizontal partitioning</b>  <math>253 - 117</math>  <math>253 - 7 = 246</math>  <math>246 - 10 = 236</math>  <math>236 - 100 = 136</math>  <b>NB</b> Only partition the smaller number to avoid negatives.</p>	<p><b>Column partitioned method</b>  <math>253 - 117</math></p> <table style="margin-left: 100px;"> <tr><td>40</td><td>13</td></tr> <tr><td>200</td><td>+ 50 + 3</td></tr> <tr><td>- 100</td><td>+ 10 + 7</td></tr> <tr><td colspan="2"><hr/></td></tr> <tr><td>100</td><td>+ 30 + 6</td></tr> <tr><td colspan="2"><hr/></td></tr> <tr><td>136</td><td></td></tr> </table>	40	13	200	+ 50 + 3	- 100	+ 10 + 7	<hr/>		100	+ 30 + 6	<hr/>		136																															
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## Calculation Policy- Multiplication

<p><b>EYFS</b> -To be able to solve problems including doubling objects.</p> <p><b>Doubling:</b> Giving double the amount of objects.</p>	<p><b>Stage 1</b> -To be able to solve one step multiplication problems using objects, pictorial representations and arrays with support.</p> <p style="text-align: center;">  <span style="margin-left: 20px;"><b>3 lots of 2 = 6.</b></span> </p>																															
<p><b>Stage 2</b> - To understand multiplication using arrays and repeated addition.</p> <p><b>Counting</b> - Count objects by grouping them in 2s, 5s or 10s</p> <p><b>Repeated addition</b>  <math>5 \times 3 = 5 + 5 + 5</math></p>  <p><b>Arrays</b>   <math>2 \times 3 =</math></p>	<p><b>Stage 3</b> -To be able to multiply 2-digit by 1-digit using a partitioned written method.</p>																															
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## Calculation Policy- Division

<p><b>EYFS</b> - To be able to solve problems including halving and sharing.</p>	<p><b>Stage 1</b> - To be able to solve one step problems involving division, using concrete objects and pictorial representations.</p>	
<p><b>Sharing</b> - giving out objects so that everyone gets the same amount.</p>	<p><b>Halving</b> - using objects/ shapes/ pictures</p> <p><b>Sharing</b> - giving out objects so that everyone gets the same amount.</p>	
<p><b>Stage 2</b> - To understand the division (<math>\div</math>) sign as sharing/ grouping.</p>	<p><b>Stage 3</b> - To be able to divide 2-digit by 1-digit using repeated subtraction.</p>	
<p>1. Sharing/ grouping - 6 divided by 3 - 6 sweets divided between 3 people</p> <div style="text-align: center;">  </div> <p>2. Halves - half of 4 is 2 - To learn halves to 20</p> <div style="text-align: center;">  </div>	<p><b>Division as repeated subtraction</b> 12 divided by 4 = 3</p> <div style="text-align: center;">  </div> <p><b>Division by repeated addition to check</b></p> <div style="text-align: center;">  </div>	
<p><b>Stage 4</b> - To be able to divide 3-digit by 1 digit using chunking.</p>	<p><b>Stage 5</b> - To be able to divide up to 4 digits by a 1 digit number using the written method of short division.</p>	<p><b>Stage 6</b> - To be able to divide numbers with up to 4 digits by a 2 digit number using long division and interpret remainders as fractions/decimals.</p>
<p><b>Chunking on a number line</b></p> <p><math>96 \div 6</math></p> <div style="text-align: center;">  </div> <p>Answer : 16</p> <p><b>Optional Challenge - Vertical chunking</b></p> <div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <math display="block">\begin{array}{r} 16 \\ 6 \overline{) 96} \\ \underline{- 60} \\ 36 \\ \underline{- 36} \\ 0 \end{array}</math> </div> <div> <p>10x</p> <p>6x</p> </div> </div>	<p><b>Partitioning</b></p> <p>96 divided by 6 = (60 + 30 + 6) divided by 6 = 60 divided by 6 = 10 30 divided by 6 = 5 6 divided by 6 = 1 10+5+1 = 16</p>	<p><b>Short division</b></p> $\begin{array}{r} 16 \\ 6 \overline{) 96} \end{array}$
		<p><b>Long Division</b></p> $\begin{array}{r} 0327r3 \\ 6 \overline{) 1965} \\ \underline{6} \phantom{0} \\ 19 \phantom{0} \\ \underline{18} \phantom{0} \\ 16 \phantom{0} \\ \underline{12} \phantom{0} \\ 45 \\ \underline{42} \\ 3 \end{array}$ <p><math>r \frac{3}{6} = \frac{1}{2} = 0.5</math></p>